

# Blind Deconvolution

From Model-Based to Deep Learning

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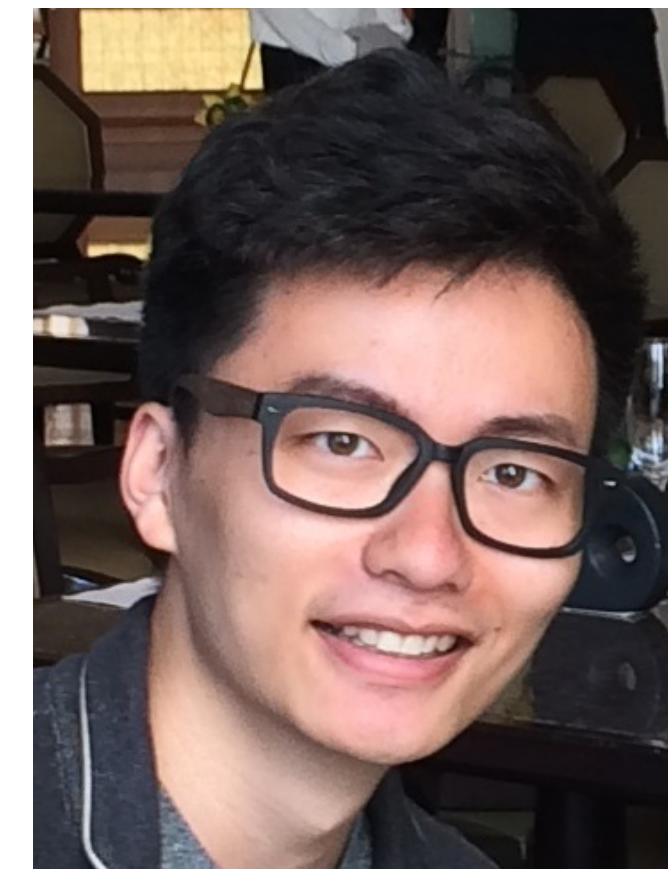
Meiguang Jin



Givi Meishvili



Stefan Roth



Zhe Hu



Daniele Perrone

NTIRE 2019 — Long Beach, CA

# Motion Blur

Motion blur is caused by object and/or camera motion during the exposure interval

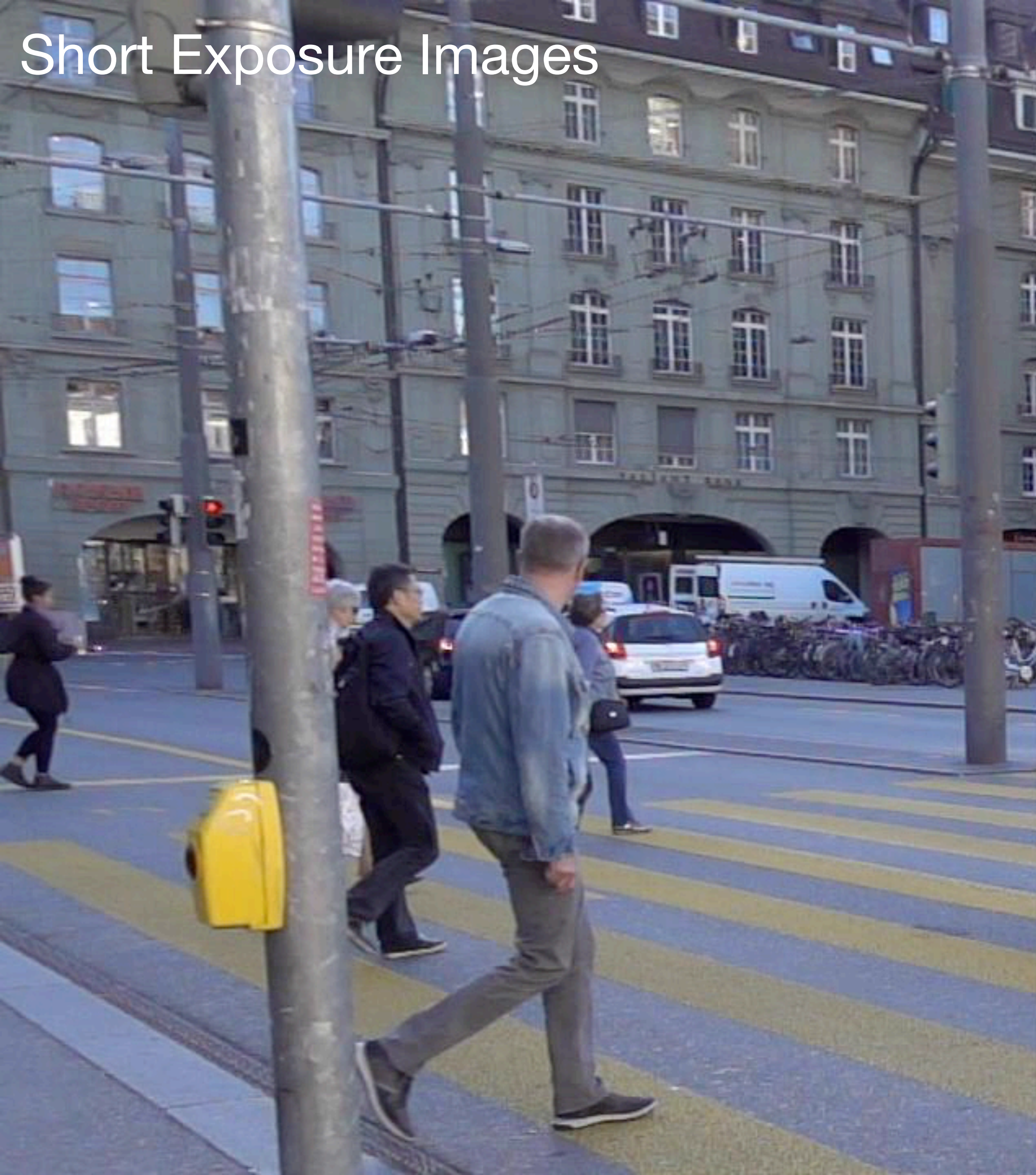


# Motion Blur

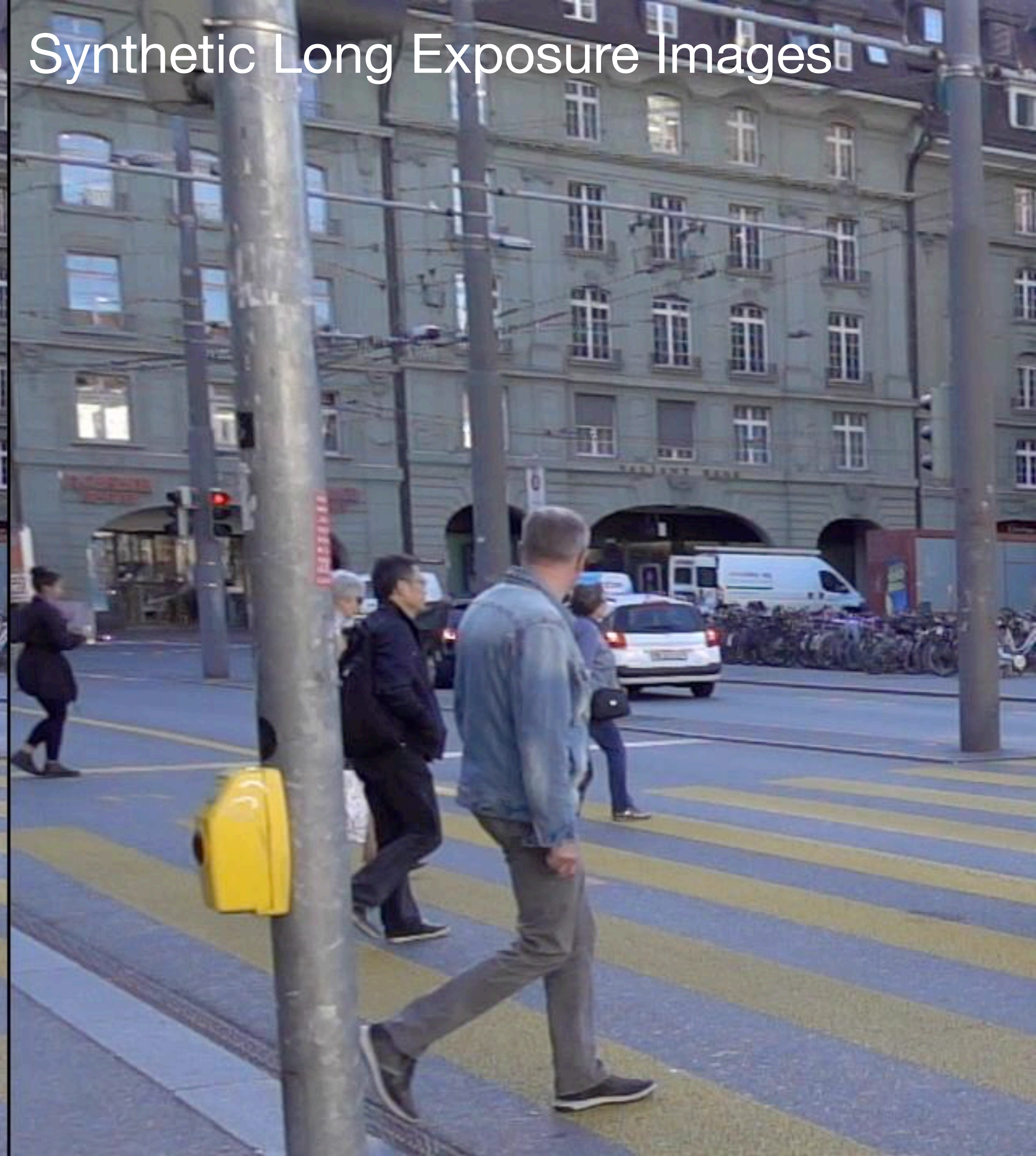
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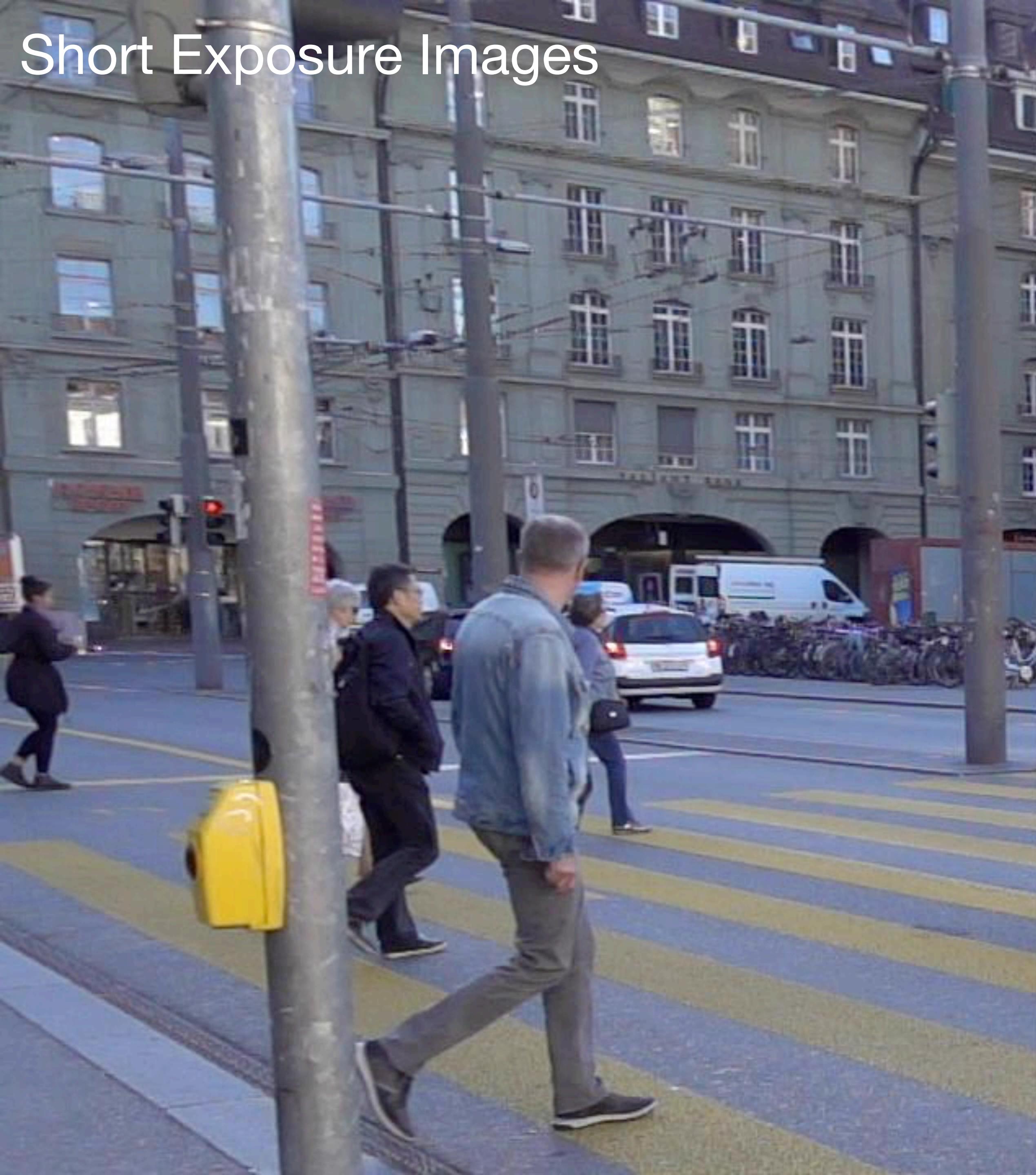
Short Exposure Images



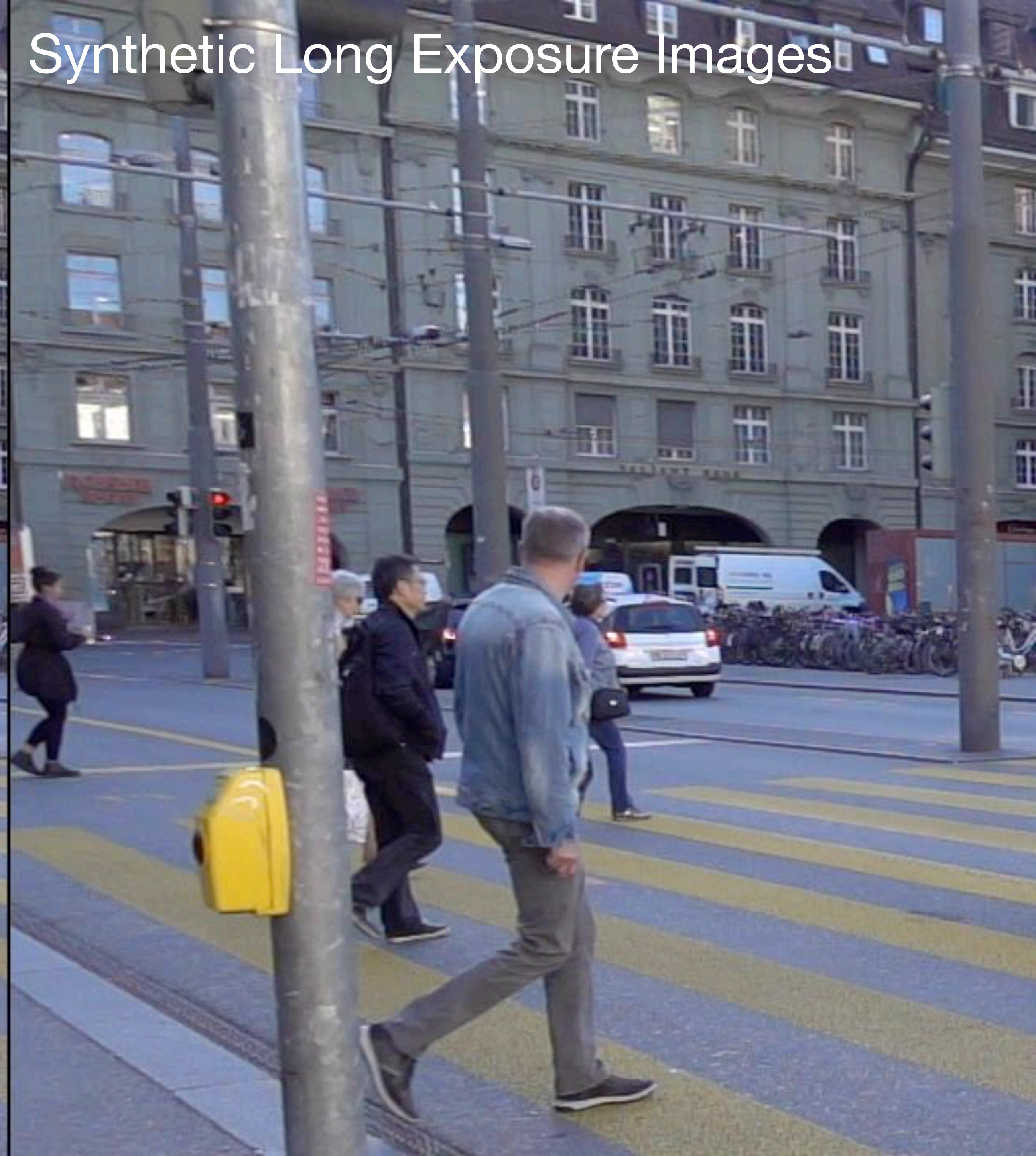
Synthetic Long Exposure Images



Short Exposure Images



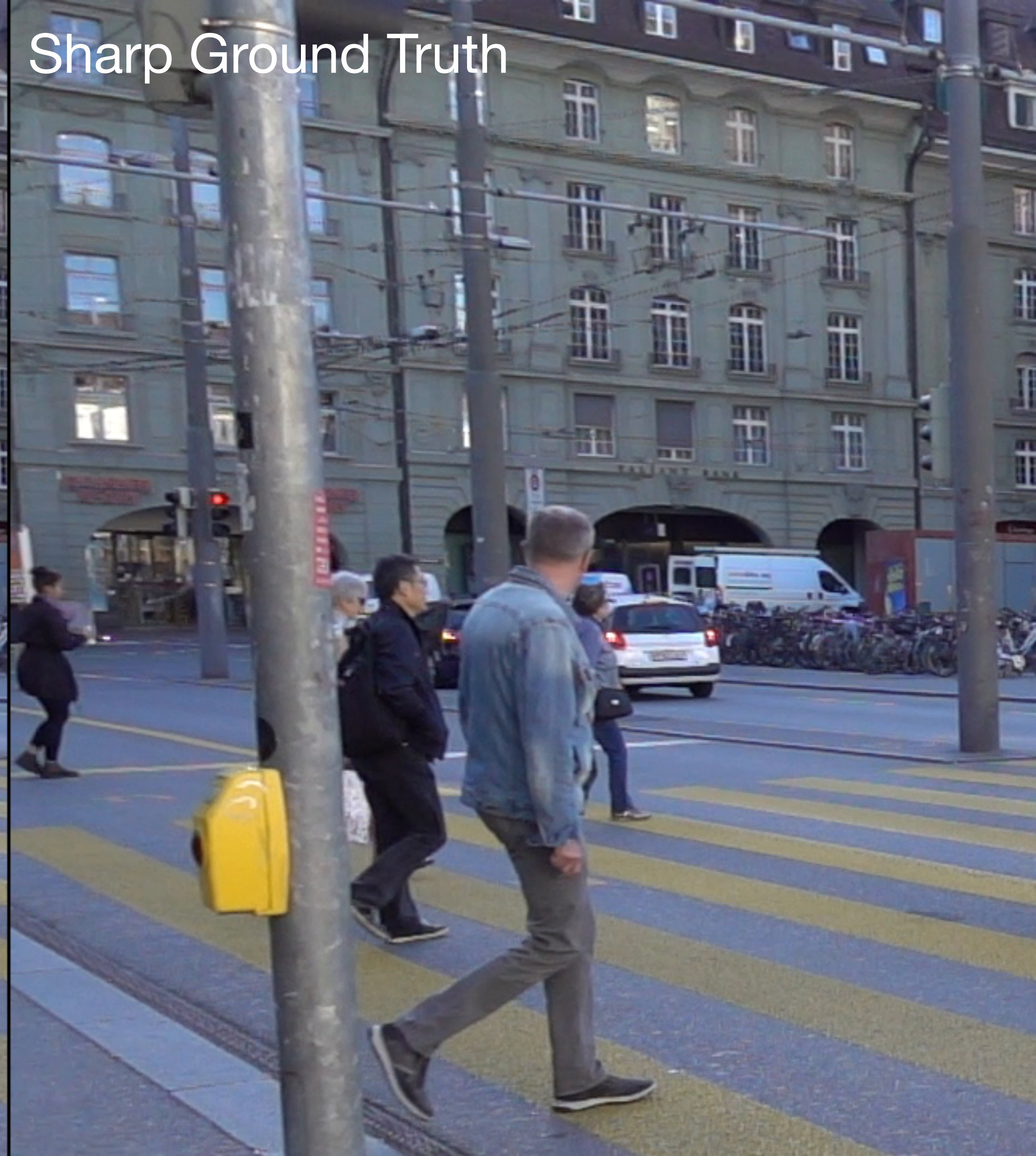
Synthetic Long Exposure Images



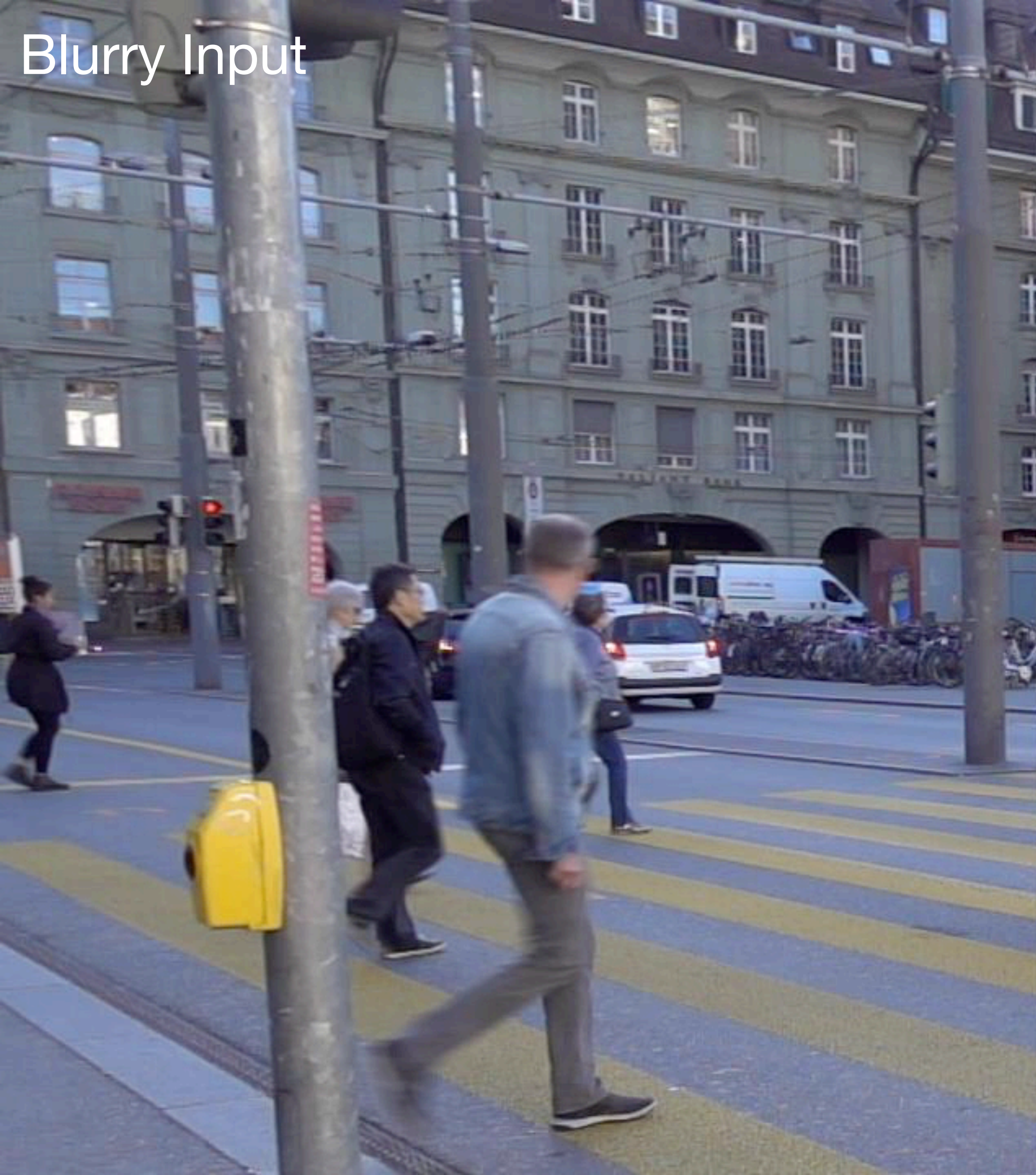
Blurry Input



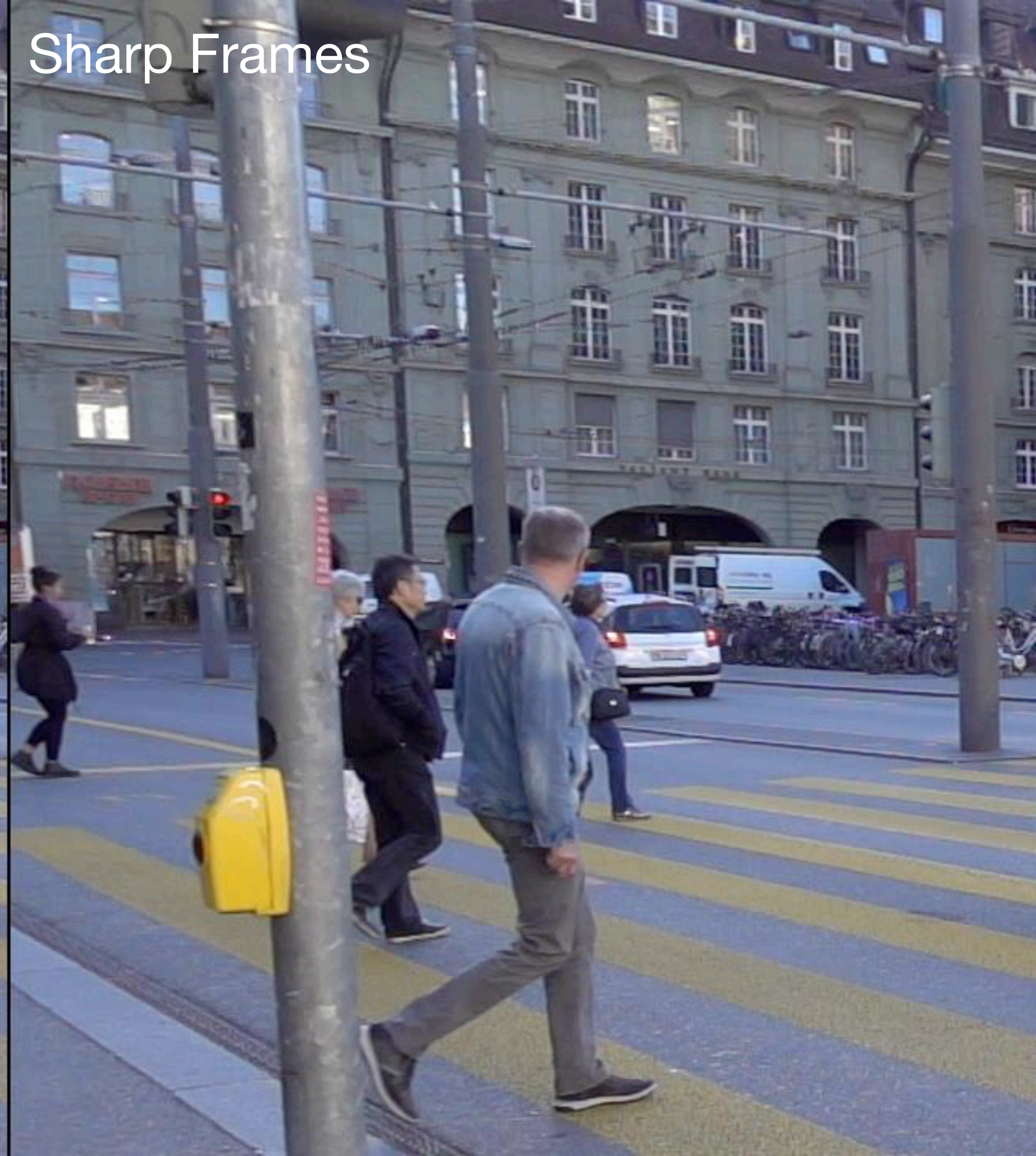
Sharp Ground Truth



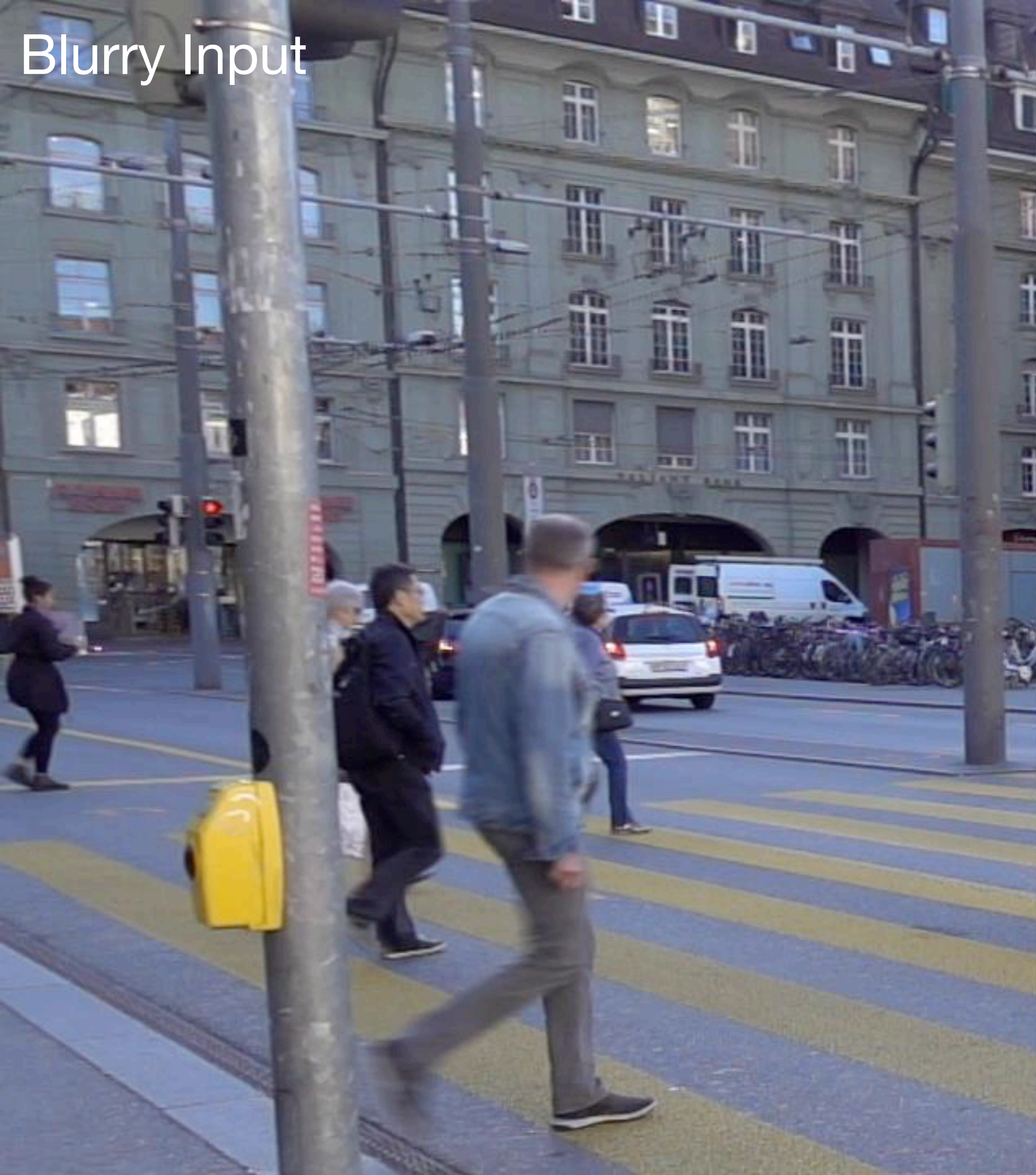
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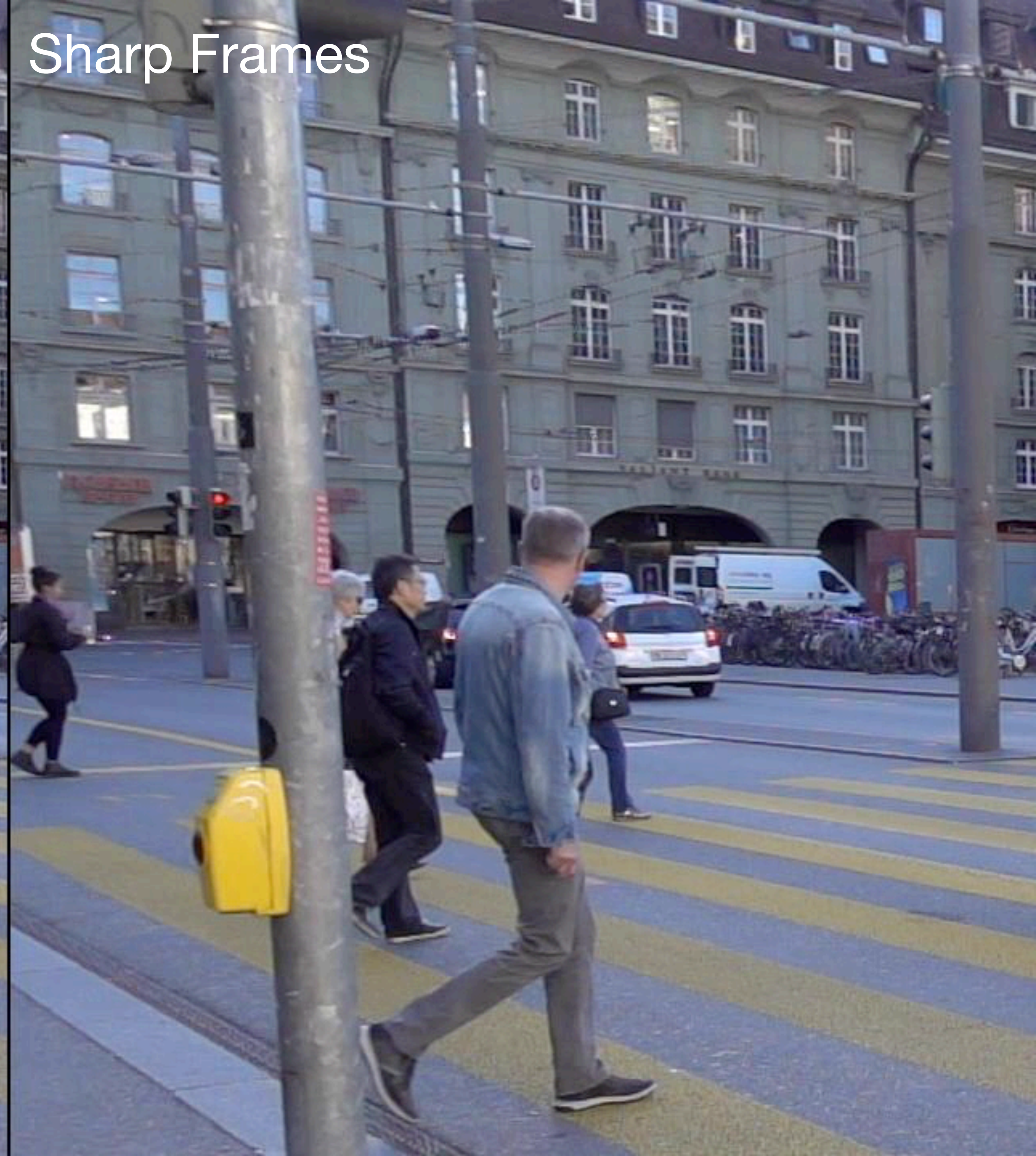
Sharp Frames



Blurry Input



Sharp Frames





# Deep learning approach

- Need to collect ground truth data: (blur image, sharp video sequence)
- Use high frame rate cameras, average frames to simulate blurry image, use the average as input and the sharp frames as output
- Need to address temporal ambiguities (eg forward or backward ordering yields the same blurry image), otherwise learning cannot succeed
- Use a sequence order-invariant loss function

Blurry Input



7 Frame Estimates



Blurry Input



7 Frame Estimates



# Blurry Input



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# Slow motion & deblurring from a blurry video

input (30 FPS)



# Slow motion & deblurring from a blurry video

output (300 FPS)



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Poster #157 - Wednesday, June 19, 15.20 – 18.00

Jin, Zhe, Favaro Learning to Extract Flawless Slow Motion from Blurry Videos CVPR 2019



# Slow motion & deblurring from a blurry video

output (300 FPS)



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# Deep learning approaches

- **pros**

- Can handle scenes of high complexity
- No need to manually design models/priors
- No need to design custom optimization procedures
- Extremely fast execution

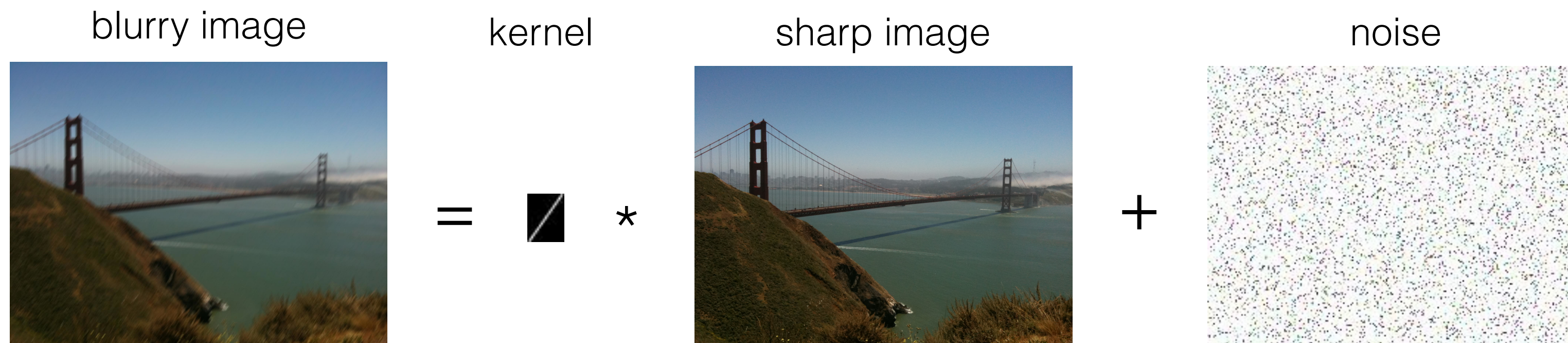
- **cons**

- Not state of the art in existing datasets (Nah et al @ -2dB PSNR from best model-based)
- No direct control/guarantees on the artifacts

# Model-based approaches

- If the camera translates along the X-Y axes and the scene is a fronto-parallel plane (or at infinity) a simple blur model is

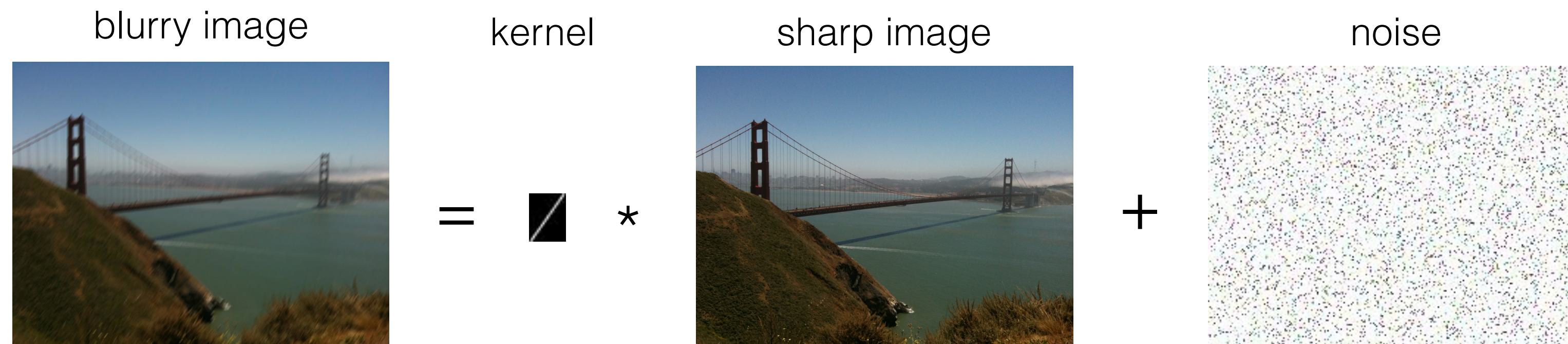
$$f = k * u + n$$



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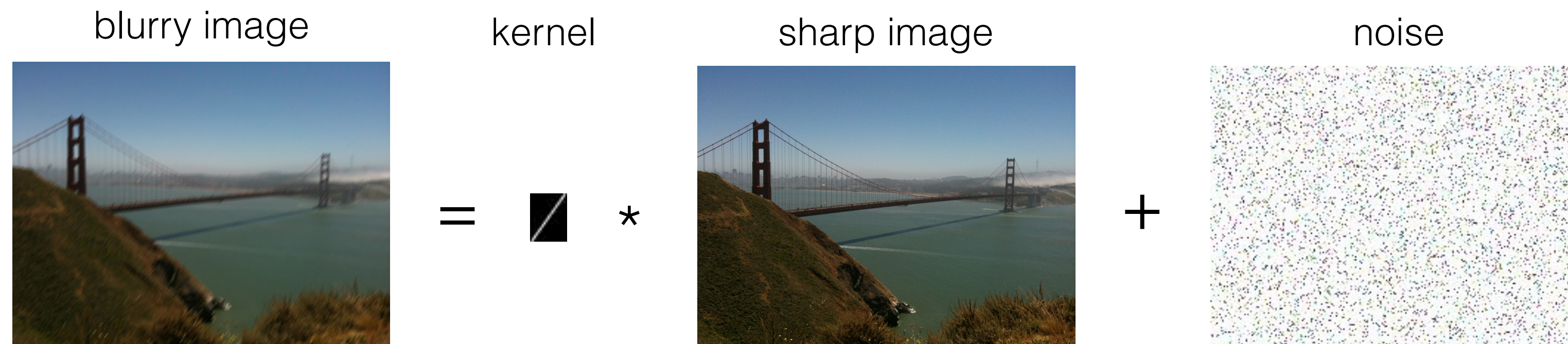
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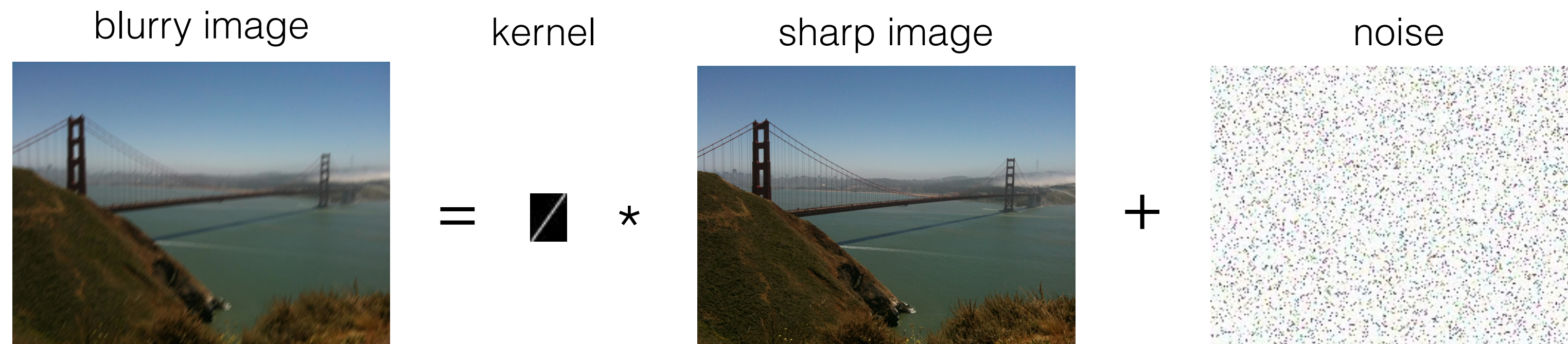
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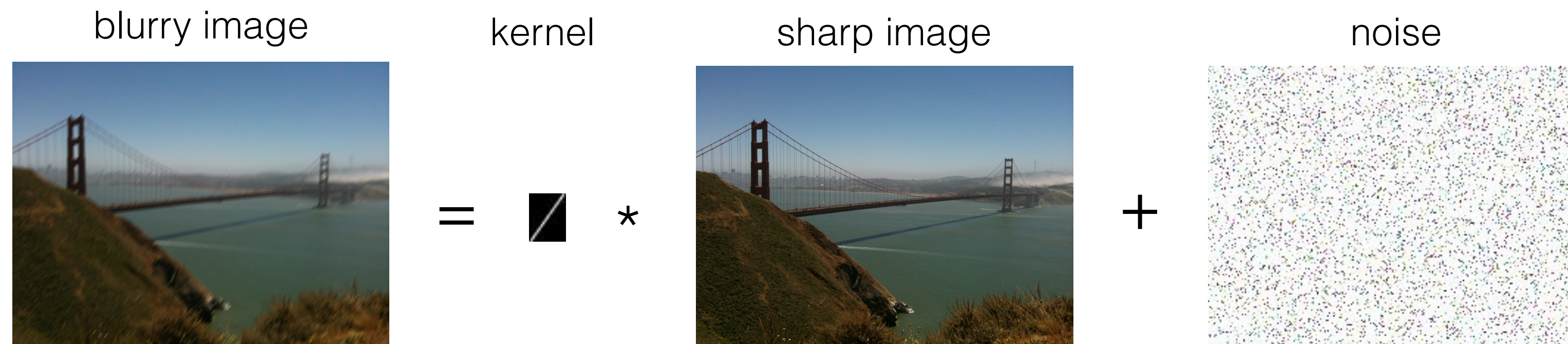
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# Blind deconvolution

- Recover **both** the blur kernel and the sharp image given the blurry image

$$f = k * u + n$$

- By using Maximum a Posteriori it can be posed as an optimization problem with some image prior (eg Total Variation\*)

$$\min_{u,k} \lambda |\nabla u|_{2,1} + \frac{1}{2} |f - k * u|_2^2$$

\*Chan and Wong *Total Variation Blind Deconvolution* TIP 1998 (also You and Kaveh 1996)



# A little problem

- The TV prior has a little flaw

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- Only the image prior is left in the cost, but the prior favors the no-blur solution!

$$|\nabla f|_{2,1} \leq |\nabla u|_{2,1}$$

# Revisiting total variation BD

- The complete problem statement is

$$\begin{aligned} \min_{u,k} \lambda |\nabla u|_{2,1} + \frac{1}{2} \|f - k * u\|_2^2 \\ \text{s.t. } k \geq 0, \quad \|k\|_1 = 1 \end{aligned}$$

where the constraints on the blur kernel ensure that the blur is non negative and adds up to 1 (or, equivalently, its  $L_1$  norm is 1)

- The  $L_1$  norm constraint fixes the scale ambiguity between  $u$  and  $k$ ; without it the minimization would make the scale of  $u$  tend to 0 and make the image prior irrelevant

# Fixing the scale ambiguity

- The complete problem statement is

$$\begin{aligned} \min_{u,k} \lambda \|\nabla u\|_{2,1} + \frac{1}{2} \|f - k * u\|_2^2 \\ \text{s.t. } k \geq 0, \quad \|k\|_1 = 1 \end{aligned}$$

- If all we need is to fix the scale of  $k$ , then  $L_p$  norms could be used too
- Would  $p \neq 1$  make a difference?

# $L_p$ normalization

- The new problem statement is

$$\begin{aligned} \min_{z,w} \quad & \lambda \|\nabla z\|_{2,1} + \frac{1}{2} \|f - w * z\|_2^2 \\ \text{s.t.} \quad & w \geq 0, \quad \|w\|_p = 1 \end{aligned}$$

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- Obtain the equivalent formulation

$$\begin{aligned} \min_{u,k} \quad & \lambda \|k\|_p \|\nabla u\|_{2,1} + \frac{1}{2} \|f - k * u\|_2^2 \\ \text{s.t.} \quad & k \geq 0, \quad \|k\|_1 = 1 \end{aligned}$$

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which has a regularization parameter that depends on the blur  $L_p$  norm

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- The equivalent formulation is almost like the previous total variation form

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$$|k|_p |\nabla u|_{2,1} \quad \text{vs} \quad |\nabla f|_{2,1}$$

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- When  $p = 2$  the term  $|k|_p < 1$  if  $k \neq \delta$  and this makes the LHS term small

# Rescuing the TV prior

- **Theorem** Assume the gradients of the true sharp image  $u$  to be i.i.d. zero-mean Gaussian and the true blur kernel  $k$  to have finite support. Given a blurry image  $f = k * u$ , the new formulation favors with high probability the true blur/image pair  $(u, k)$  over the trivial no-blur pair  $(f, \delta)$  for  $p \geq 2$ .

# Optimization

- We use the Frank-Wolfe algorithm and alternate between blur and image
- Advantages
  1. For the first time it is possible to optimize the cost function exactly
  2. Coarse to fine scheme is not needed
  3. Careful initialization is not necessary (can start with  $k = \delta$ )
  4. Regularization parameter is not changed during the iteration time
  5. The formulation is convex separately in each variable

# Quantitative evaluation

**Table 1:** Quantitative comparison on the entire SUN dataset [39] (640 blurry images).

Method	mean error ratio	maximum error ratio	failure cases
Cho & Lee [7]	9.198	113.491	224
Krishnan <i>et al.</i> [20]	12.015	142.668	475
Levin <i>et al.</i> [23]	6.695	44.171	357
Sun <i>et al.</i> [39]	2.581	35.765	44
Xu & Jia [44]	3.817	75.036	98
Perrone & Favaro [31]	2.114	8.517	<b>7</b>
Chakrabarti [4]	3.062	11.576	64
Michaeli & Irani [24]	2.617	9.185	30
Pan <i>et al.</i> [29]	<b>1.914</b>	23.279	11
PN	2.299	<b>6.764</b>	8
FW	2.195	<b>6.213</b>	8

Sum of squared differences ratio  $\frac{|u - \hat{u}|^2}{|u - \hat{u}_*|^2}$   $\hat{u}_*$  estimated with GT kernel  
 $\hat{u}$  estimated with estimated kernel



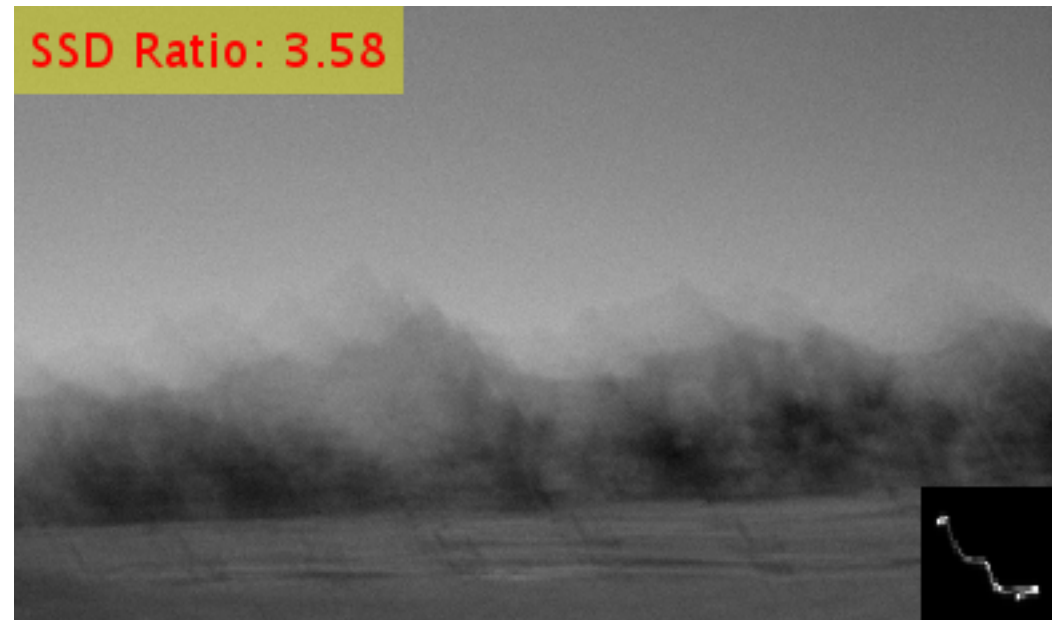
# Quantitative evaluation

**Table 2:** Quantitative comparison on the small BSDS dataset [1] (72 blurry images).

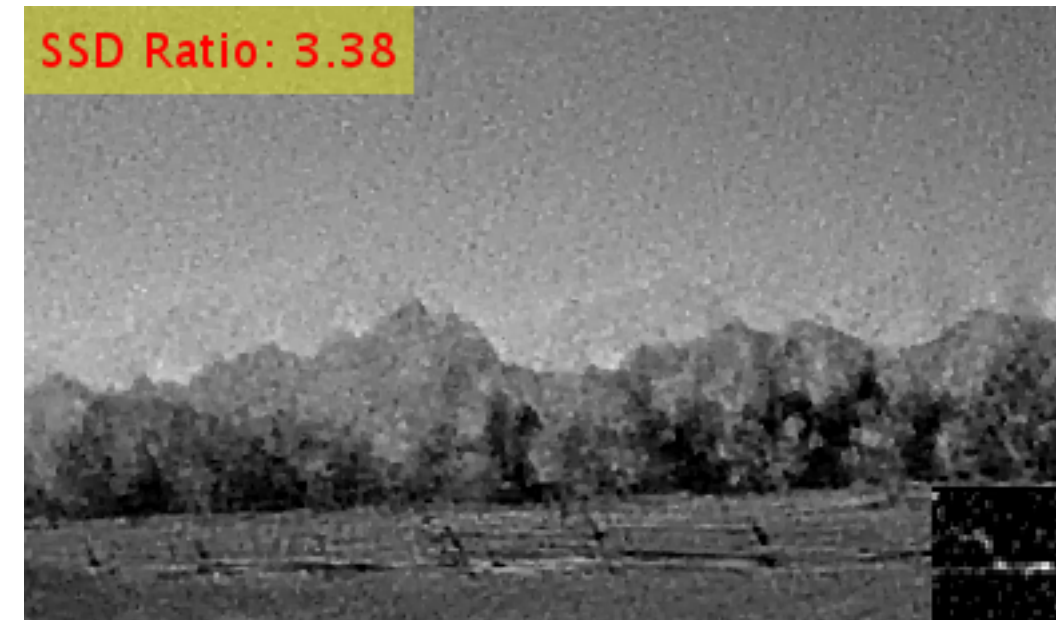
Method	mean error ratio	maximum error ratio	failure cases
Sun <i>et al.</i> [39]	2.648	15.152	12
Xu & Jia [44]	3.645	22.272	13
Perrone & Favaro [31]	2.093	7.493	4
Chakrabarti [4]	3.768	11.809	9
Michaeli & Irani [24]	3.458	23.001	14
Pan <i>et al.</i> [29]	2.058	13.516	3
Yan <i>et al.</i> [46]	2.022	12.237	3
$L^1$ normalization	2.211	7.821	3
weight decay (heuristic)	2.591	8.762	2
$L^2$ blur prior (classic)	2.487	7.953	4
PN	2.011	4.676	<b>0</b>
FW	<b>1.983</b>	<b>4.387</b>	<b>0</b>

Sum of squared differences ratio  $\frac{|u - \hat{u}|^2}{|u - \hat{u}_*|^2}$   $\hat{u}_*$  estimated with GT kernel  
 $\hat{u}$  estimated with estimated kernel

# Qualitative comparisons



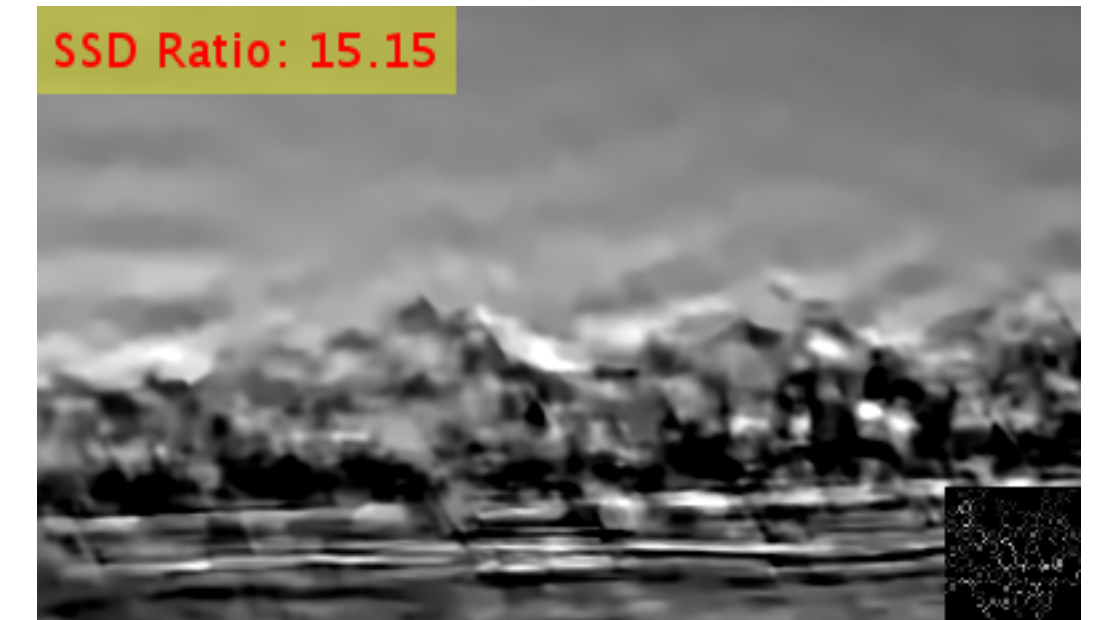
input



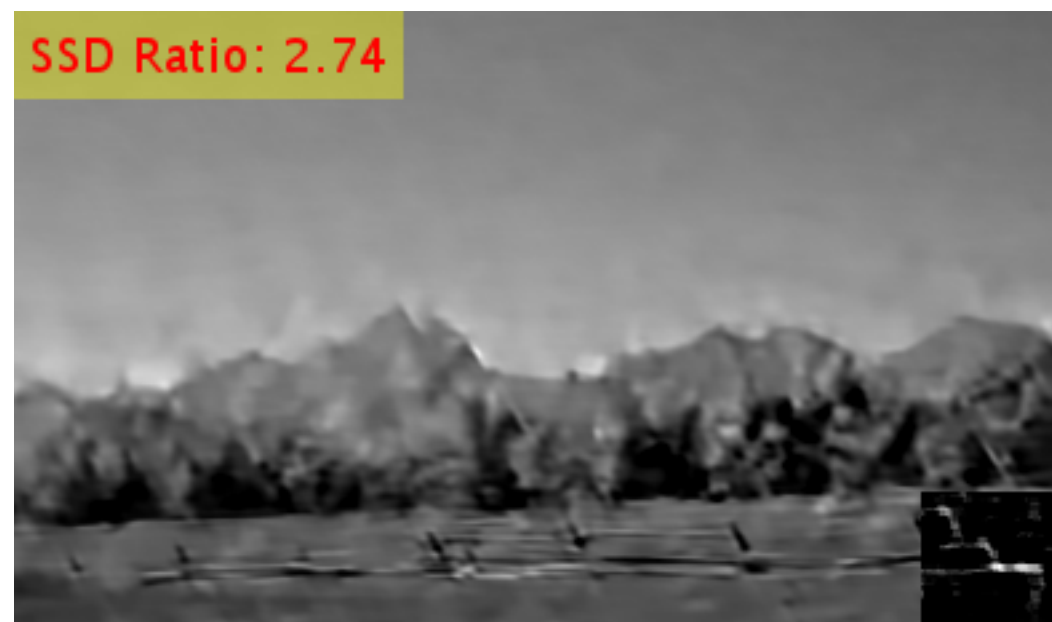
Xu and Jia 2010



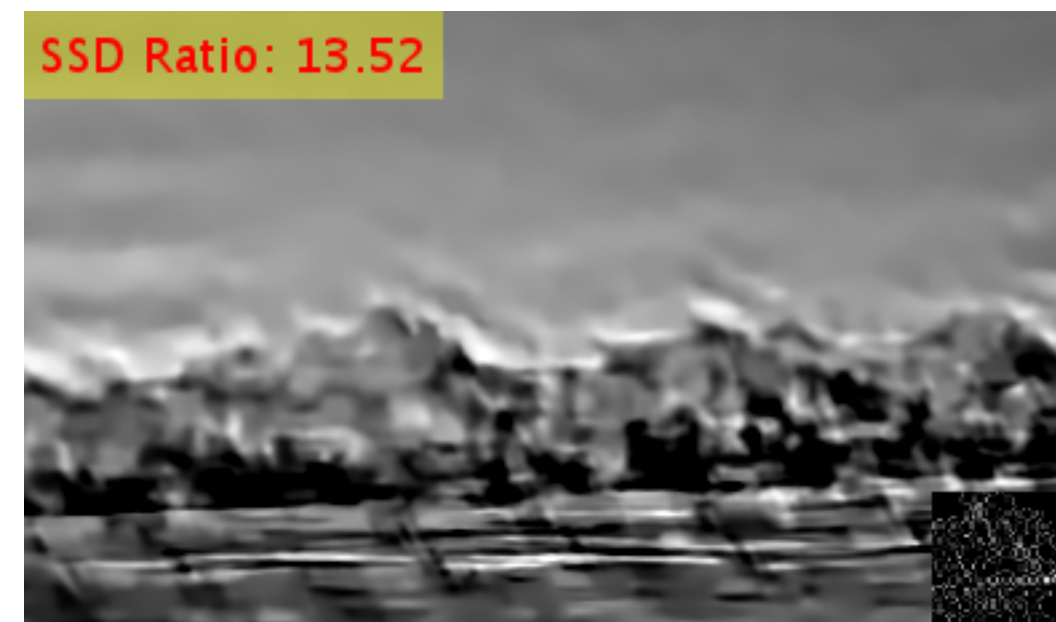
Chakrabarti 2016



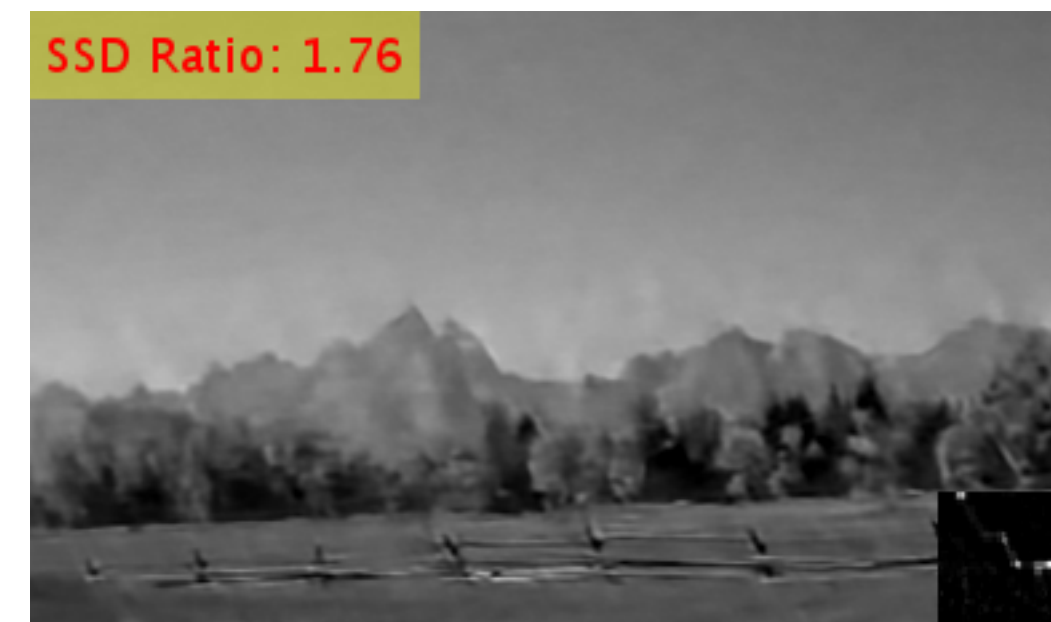
Sun et al 2013



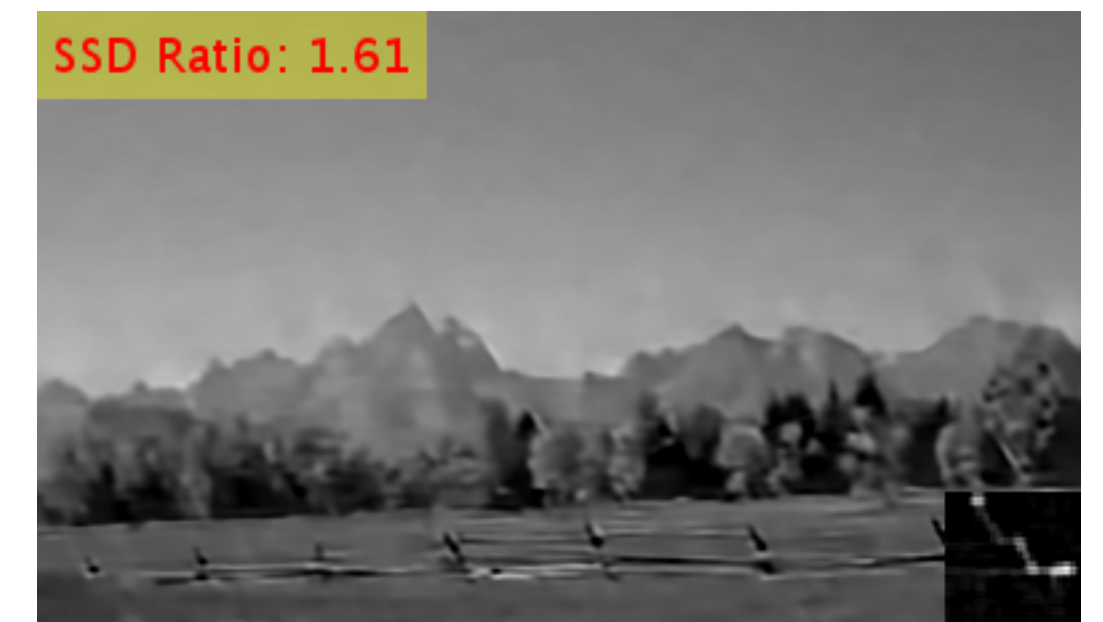
Michaeli and Irani 2014



Pan et al 2016



Perrone and Favaro 2016



FW

# Worst cases in real images



input



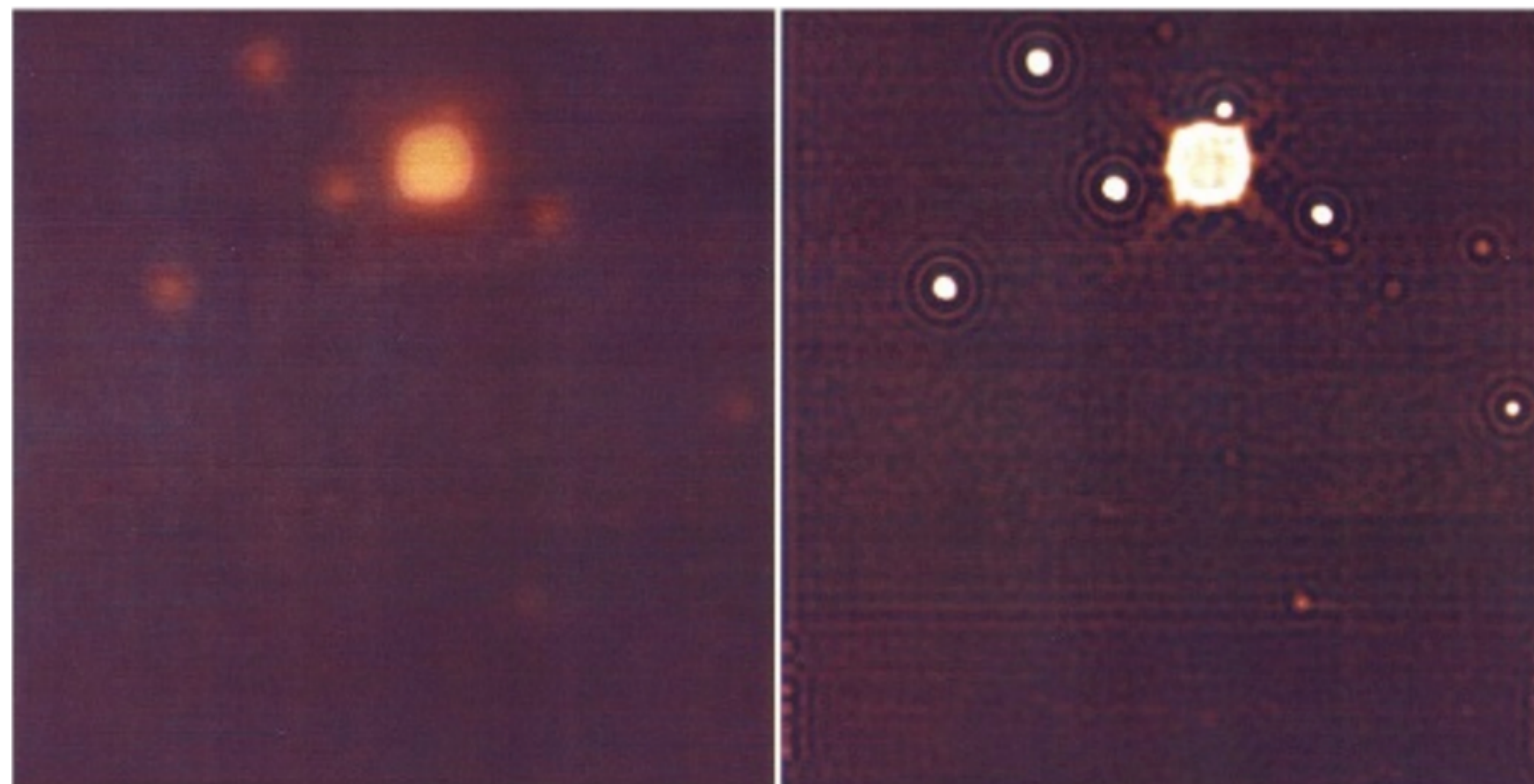
Pan et al 2016



PN

# Conclusions

- Deep learning methods will probably prevail in the end
- There are some limitations that might take time to address
- Can we trust that the reconstruction is not a hallucination of the data?



Acquired Image

After Deconvolution



# Conclusions

- In contrast model-based methods are easily interpretable
- There is still quite a bit to do even with simple formulations
- It pays to pay attention to the details

Blurry Input



7 Frame Estimates



Blurry Input



7 Frame Estimates

